AHSAA Homeschool Student Eligibility Exams Algebra I

| Standard Reference | Standard Text | Percentage of Test Items |
| :---: | :---: | :---: |
|  | Number and Quantity and Algebra | 50\% |
| N | Number and Quantity |  |
| N-RN | The Real Number System |  |
|  | Extend the properties of exponents to rational exponents. |  |
| N-RN. 1 | Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents. [N-RN1] Example: We define $5^{1 / 3}$ to be the cube root of 5 because we want $\left(5^{1 / 3}\right)^{3}=$ $5^{(1 / 3) 3}$ to hold, so $\left(5^{1 / 3}\right)^{3}$ must equal 5. |  |
| N-RN. 2 | Rewrite expressions involving radicals and rational exponents using the properties of exponents. [N-RN2] |  |
|  | Use properties of rational and irrational numbers. |  |
| N-RN. 3 | Explain why the sum or product of two rational numbers is rational; that the sum of a rational number and an irrational number is irrational; and that the product of a nonzero rational number and an irrational number is irrational. [N-RN3] |  |
| N-Q | Quantities |  |
|  | Reason quantitatively and use units to solve problems. |  |
| N-Q. 4 | Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays. [ $\mathrm{N}-\mathrm{Q} 1$ ] |  |
| N-Q. 5 | Define appropriate quantities for the purpose of descriptive modeling. [ N Q2] |  |
| N-Q. 6 | Choose a level of accuracy appropriate to limitations on measurement when reporting quantities. [ $\mathrm{N}-\mathrm{Q} 3$ ] |  |
| A | Algebra |  |
| A-SSE | Seeing Structure in Expressions |  |
|  | Interpret the structure of expressions. (For standard 7 linear, exponential, quadratic; for standard 8 linear, exponential, quadratic, rational.) |  |
| A-SSE. 7 | Interpret expressions that represent a quantity in terms of its context. * [ASSE1] |  |
| A-SSE.7.a | Interpret parts of an expression, such as terms, factors, and coefficients. [A-SSE1a] |  |
| A-SSE.7.b | Interpret complicated expressions by viewing one or more of their parts as a single entity. [A-SSE1b] <br> Example: Interpret $P(1+r)^{n}$ as the product of $P$ and a factor not depending on $P$. |  |


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| A-SSE. 8 | Use the structure of an expression to identify ways to rewrite it. [A-SSE2] Example: See $x^{4}-y^{4}$ as $\left(x^{2}\right)^{2}-\left(y^{2}\right)^{2}$, thus recognizing it as a difference of squares that can be factored as $\left(x^{2}-y^{2}\right)\left(x^{2}+y^{2}\right)$. |  |
|  | Write expressions in equivalent forms to solve problems. (Quadratic and exponential.) |  |
| A-SSE. 9 | Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. * [ASSE3] |  |
| A-SSE.9.a | Factor a quadratic expression to reveal the zeros of the function it defines. [A-SSE3a] |  |
| A-SSE.9.b | Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines. [A-SSE3b] |  |
| A-SSE.9.c | Determine a quadratic equation when given its graph or roots. |  |
| A-SSE.9.d | Use the properties of exponents to transform expressions for exponential functions. [A-SSE3c] <br> Example: The expression $1.15^{t}$ can be rewritten as $\left(1.15^{1 / 12}\right)^{12 t} \approx 1.012^{12 t}$ to reveal the approximate equivalent monthly interest rate if the annual rate is $15 \%$. |  |
| A-APR | Arithmetic with Polynomials and Rational Expressions |  |
|  | Perform arithmetic operations on polynomials |  |
| A-APR. 10 | Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials. [A-APR1] |  |
|  | Rewrite rational expressions. (Linear and quadratic denominators.) |  |
| $\begin{array}{\|l} \hline \text { A-APR. } 11 \\ \hline \text { A-CED } \\ \hline \end{array}$ | Understand that rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression; add, subtract, multiply, and divide rational expressions. [A-APR7] |  |
|  | Creating Equations* |  |
|  | Create equations that describe numbers or relationships. (Linear, quadratic, and exponential (integer inputs only); for Standard 14, linear only.) |  |
| A-CED. 12 | Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions. [A-CED1] |  |
| A-CED. 13 | Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. [A-CED2] |  |


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|  | Represent constraints by equations or inequalities, and by systems of <br> equations and/or inequalities, and interpret solutions as viable or non- <br> viable options in a modeling context. [A-CED3] <br> Example: Represent inequalities describing nutritional and cost constraints <br> on combinations of different foods. |  |
| A-CED.14 | Rearrange formulas to highlight a quantity of interest, using the same <br> reasoning as in solving equations. [A-CED4] <br> Example: Rearrange Ohm's law $V=$ IR to highlight resistance $R$. |  |
| A-CED.15 | Reasoning with Equations and Inequalities | Understand solving equations as a process of reasoning and explain the <br> reasoning. (Master linear; learn as general principle.) |
| A-REI | Explain each step in solving a simple equation as following from the <br> equality of numbers asserted at the previous step, starting from the <br> assumption that the original equation has a solution. Construct a viable <br> argument to justify a solution method. [A-REI1] |  |
| A-REI.16 | Solve equations and inequalities in one variable. (Linear inequalities; literal <br> that are linear in the variables being solved for; quadratics with real <br> solutions.) |  |
| A-REI.17 | Solve linear equations and inequalities in one variable, including equations <br> with coefficients represented by letters. [A-REI3] |  |
| A-REI.18 | Solve quadratic equations in one variable. [A-REI4] | Ase the method of completing the square to transform any quadratic <br> equation in x into an equation of the form ( $x$ - p) $=q$ that has the same <br> solutions. Derive the quadratic formula from this form. [A-REI4a] |
| A-REI.18.a | Solve quadratic equations by inspection (e.g., for $\left.x^{2}=49\right)$, taking square <br> roots, completing the square, the quadratic formula and factoring, as <br> appropriate to the initial form of the equation. Recognize when the <br> quadratic formula gives complex solutions and write them as a $\pm$ bi for real <br> numbers a and b. [A-REI4b] |  |
| A-REI.19 | Solve systems of equations. (Linear-linear and linear-quadratic.) | Prove that, given a system of two equations in two variables, replacing one <br> equation by the sum of that equation and a multiple of the other produces <br> a system with the same solutions. [A-REI5] |


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|  | Represent and solve equations and inequalities graphically. (Linear and exponential; learn as general principle.) |  |
| A-REI. 22 | Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line). [A-REI10] |  |
| A-REI. 23 | Explain why the $x$-coordinates of the points where the graphs of the equations $y=f(x)$ and $y=g(x)$ intersect are the solutions of the equation $f(x)=g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.* [A-REI11] |  |
| A-REI. 24 | Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes. [A-REI12] |  |
| F | Functions | 40\% |
| F-IF | Interpreting Functions |  |
|  | Understand the concept of a function and use function notation. (Learn as general principle; focus on linear and exponential and on arithmetic and geometric sequences.) |  |
| F-IF. 25 | Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If $f$ is a function and $x$ is an element of its domain, then $f(x)$ denotes the output of $f$ corresponding to the input $x$. The graph of $f$ is the graph of the equation $y=f(x)$. [F-IF1] |  |
| F-IF. 26 | Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. [FIF2] |  |
| F-IF. 27 | Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. [F-IF3] <br> Example: The Fibonacci sequence is defined recursively by $f(0)=f(1)=1$, $f(n+1)=f(n)+f(n-1)$ for $n \geq 1$. |  |
|  | Interpret functions that arise in applications in terms of the context. (Linear, exponential, and quadratic.) |  |
| F-IF. 28 | For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* [F-IF4] |  |


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| F-IF. 29 | Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.* [F-IF5] <br> Example: If the function $h(n)$ gives the number of person-hours it takes to assemble $n$ engines in a factory, then the positive integers would be an appropriate domain for the function. |  |
| F-IF. 30 | Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph. * [F-IF6] |  |
|  | Analyze functions using different representations. (Linear, exponential, quadratic, absolute value, step, and an awareness of piecewise-defined.) |  |
| F-IF. 31 | Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* [F-IF7] |  |
| F-IF.31.a | Graph linear and quadratic functions and show intercepts, maxima, and minima. [F-IF7a] |  |
| F-IF.31.b | Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions. [F-IF7b] |  |
| F-IF. 32 | Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. [F-IF8] |  |
| F-IF.32.a | Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context. [F-IF8a] |  |
| F-IF.32.b | Use the properties of exponents to interpret expressions for exponential functions. [F-IF8b] <br> Example: Identify percent rate of change in functions such as $y=(1.02)^{t}, y=$ $(0.97)^{t}, y=(1.01)^{12 t}$, and $y=(1.2)^{t / 10}$, and classify them as representing exponential growth and decay. |  |
| F-IF. 33 | Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). [F-IF9] <br> Example: Given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum. |  |
| F-BF | Building Functions |  |
|  | Build a function that models a relationship between two quantities. (For standards 34 and 35 , linear, exponential, and quadratic.) |  |
| F-BF. 34 | Write a function that describes a relationship between two quantities.* [FBF1] |  |
| F-BF.34.a | Determine an explicit expression, a recursive process, or steps for calculation from a context. [F-BF1a] |  |


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| F-BF.34.b | Combine standard function types using arithmetic operations. [F-BF1b] Example: Build a function that models the temperature of a cooling body by adding a constant function to a decaying exponential, and relate these functions to the model. |  |
| F-BF. 35 | Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms. * [F-BF2] |  |
|  | Build new functions from existing functions. (Linear, exponential, quadratic, and absolute value.) |  |
| F-BF. 36 | Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. [F-BF3] |  |
| F-LE | Linear, Quadratic, and Exponential Models* |  |
|  | Construct and compare linear, quadratic, and exponential models and solve problems |  |
| F-LE. 37 | Distinguish between situations that can be modeled with linear functions and with exponential functions. [F-LE1] |  |
| F-LE.37.a | Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals. [F-LE1a] |  |
| F-LE.37.b | Recognize situations in which one quantity changes at a constant rate per unit interval relative to another. [F-LE1b] |  |
| F-LE.37.c | Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another. [F-LE1c] |  |
| F-LE. 38 | Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table). [F-LE2] |  |
| F-LE. 39 | Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function. [F-LE3] |  |
|  | Interpret expressions for functions in terms of the situation they model. (Linear and exponential of form $f(x)=b^{x}+k$.) |  |
| F-LE. 40 | Interpret the parameters in a linear or exponential function in terms of a context. [F-LE5] |  |
| S | Statistics and Probability | 10\% |
| S-ID | Interpreting Categorical and Quantitative Data |  |
|  | Summarize, represent, and interpret data on a single count or measurement variable |  |
| S-ID. 41 | Represent data with plots on the real number line (dot plots, histograms, and box plots). [S-ID1] |  |


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| S-ID.42 | Use statistics appropriate to the shape of the data distribution to compare <br> center (median, mean) and spread (interquartile range, standard deviation) <br> of two or more different data sets. [S-ID2] |  |
| S-ID.43 | Interpret differences in shape, center, and spread in the context of the <br> data sets, accounting for possible effects of extreme data points (outliers). <br> [S-ID3] | Summarize, represent, and interpret data on two categorical and <br> quantitative variables. (Linear focus, discuss general principle.) |
|  | Summarize categorical data for two categories in two-way frequency <br> tables. Interpret relative frequencies in the context of the data (including <br> joint, marginal, and conditional relative frequencies). Recognize possible <br> associations and trends in the data. [S-ID5] |  |
| S-ID.44 | Fit a function to the data; use functions fitted to data to solve problems in <br> the context of the data. Use given functions or choose a function suggested <br> by the context. Emphasize linear, quadratic, and exponential models. [S- <br> ID6a] |  |
| S-ID.45.a | Informally assess the fit of a function by plotting and analyzing residuals. <br> [S-ID6b] |  |
| S-ID.45.b | Fit a linear function for a scatter plot that suggests a linear association. [S- <br> ID6c] |  |
| S-ID.45.c | Interpret linear models |  |
| S-ID.46 | Interpret the slope (rate of change) and the intercept (constant term) of a <br> linear model in the context of the data. [S-ID7] |  |
| S-CP | Conditional Probability and the Rules of Probability <br> S-CP.47Understand independence and conditional probability and use them to <br> interpret data. (Link to data from simulations or experiments.) | Understand that two events A and B are independent if the probability of A <br> and B occurring together is the product of their probabilities, and use this <br> (haracterization to determine if they are independent. [S-CP2] |

